

Creating mathematical jigsaw puzzles using T_EX and friends

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Outline

- 1 Motivation
 - What is a 'Mathematical Jigsaw'?
 - Existing software
 - CMEP and its needs
- 2 The new software
 - Design goals
 - The implementation
- 3 Open problems and future directions

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What is a 'Mathematical Jigsaw'?

- Used in classrooms for variety of purposes:
- Jigsaws and dominoes: A more enjoyable way to practise skills; can involve logical reasoning too
- Card sorts: Sort into groups or into order

Examples

- Jigsaw (dark blue)
 - Sides match if the question gives the answer
 - A '?' means an answer is not given – you have to work it out
 - The outside edges of the puzzle will not match anything
 - Ignore the small circled numbers
- Card sort (pale blue)
 - Order these to prove that $\sqrt{2}$ is irrational
 - Again ignore the small circled numbers
- Follow-me cards or dominoes (yellow)
 - These form a continuous loop, joining question to answer
 - In a class, each student has some of the cards to read out

Examples (Answers)

- Jigsaw (dark blue)
 - Printed solution sheet
- Card sort (pale blue)
 - $2 - 5 - 6 - 7 - 9 - 3 - 8 - 4 - 1$
- Follow-me cards or dominoes (yellow)
 - No answers offered!

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Existing software

- Formulator Tarsia
 - Created by Hermitech Laboratory
 - Free (as in beer)
 - Windows-only
 - MathML-based
 - Graphical frontend
 - Very popular in schools in UK
 - Many resources (activities) available to download

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What is CMEP?

- Cambridge Mathematics Education Project
- Creating rich, engaging, coherent mathematics resources for 16–18 year olds
- In development phase
- Public website launch planned for early 2015
- Resources will include card sorts and perhaps jigsaws

Why not use Formulator Tarsia?

- Windows-based; CMEP developers use Mac or Linux
- I prefer $\text{T}_{\text{E}}\text{X}$ output quality to Tarsia output
- More flexibility and control with $\text{T}_{\text{E}}\text{X}$
- Tarsia content cannot be easily imported or exported
- Tarsia is semi-WYSIWYG so harder to input than $\text{T}_{\text{E}}\text{X}$
- Need output in printable form and Markdown for automated conversion to HTML

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User needs

- Easy to input content
- Flexibility to have different layouts, fonts, etc.
- Flexibility to easily change format of puzzle
- Preferably text-based input files
- Knowledge of \LaTeX can be assumed, but nothing more
- Easy to generate jigsaws, etc., from input files

Software goals

- Operating-system agnostic (at least Mac & Linux)
- Easy to install and use
- Minimum of non-standard dependencies
- Easy to maintain and extend (time constraints)
- Can produce Markdown output for converting into webpages

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The implementation

- Data input files: YAML
- \LaTeX template files: Use TikZ
- Data structure template files: YAML
- Processing software: Python 3.x, calls `(lua)latex` to typeset
- In alpha state

Example data file

- Title and type specification
- Layout specification (overriding defaults)
- Content data

Example data file: Title and type specification

```
# Proving  $\sqrt{2}$  is irrational  
type: cardsort  
title:  $\sqrt{2}$  is irrational  
note: Sort the cards into order to prove ...
```

Example data file: Layout specification

```
# puzzle size  
rows: 6  
columns: 1  
# Do we shuffle the order of the cards from  
# the order given when producing the problem?  
# Say "true" for a proof sorting activity.  
# It probably does not make sense to say  
# "false" here but still to produce a solution.  
shuffleCards: true  
# Does this puzzle require production of a  
# solution? If so, the cards must be given  
# in the correct order initially.  
produceSolution: true
```

Example data file: Layout specification

```
# Default text size on cards
textSize: 6
# Card title
cardTitle: CMEP --  $\sqrt{2}$  is irrational
cardTitleSize: 2

# Use CMEP Markdown output
puzzleTemplateMarkdown:
  template-cardsort-puzzle-CMEP-1col.md
solutionTemplateMarkdown:
  template-cardsort-solution-CMEP-1col.md
```

Example data file: Content data

cards:

- Suppose, for a contradiction, that ...
- That is, we can write $\sqrt{2} = \dots$
- Squaring, we have $2 = \frac{m^2}{n^2}$.
- Multiply across to get $2n^2 = m^2$.
- In the prime factorisations of m^2 ...
- In the prime factorisation of $2n^2$, ...
- But prime factorisations are unique, so ...
- This is a contradiction, so our original ...
- So $\sqrt{2}$ is irrational.

Other niceties

- Can number cards
- Hidden or different puzzle data (e.g., '?' in puzzle)
- Can handle images

Open problems

- How do I store and locate configurations on different OSes?
 - Standard template files
 - User template files
 - Software to work identically on Mac, Linux and even Windows?
- How do I create a 'package' for each of the different OSes which can be simply installed?

Future directions

- Write documentation!
- Allow for command-line and configuration file configuration
- If really wanted, create a graphical data editor.
 - But I think text-based file is simpler to edit.

Obtaining the software

- `https://github.com/juliangilbey/jigsaw-generator`
- **Email me at** `J.Gilbey@maths.cam.ac.uk` **or**
`jdg@debian.org`